

# Noble Deceit: Optimizing Social Welfare for Myopic Multi-Armed Bandits

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## Approach and Key Ideas

**Goal:** determine the best arm by exploring each arm  
Divide into phases: In the  $k$ -phase, we explore  $a_k$

What if an agent is recommended  $a_k$ ?

- **Key Information Asymmetry:** agents don't know if they're exploring or exploiting:
  - Might be first to explore  $a_k$  -- incur some **cost**
  - Maybe  $a_k$  was explored by a previous agent and found to be better than  $a_i$  -- get some **benefit**
- Design  $k$ -phase to balance these two factors

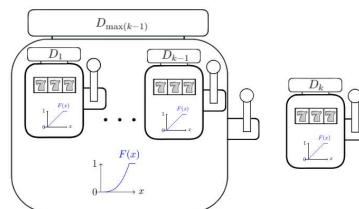
**Structure of the  $k$ -phase:**

- Partition support of  $D_{\max(k-1)} = \max\{D_1, \dots, D_{k-1}\}$  into a set of intervals  $\{I_t\}$
- Let  $a_i$  be the best arm among  $\{a_1, \dots, a_{k-1}\}$
- Each agent  $t$  will explore  $a_k$  iff  $r_i \in I_t$
- Before Exploration: agents exploit  $a_i$
- After Exploration: agents pull the better of  $a_k$  and  $a_i$

This works if agents view the value of  $a_i$  as a random draw from  $D_{\max(k-1)}$ , i.e. they can't learn anything about what happened in previous phases

**Ensure phases are independent:**

- $k$ -phase ends only when it is certain that  $a_k$  would have been explored irrespective of realizations of arms
- the length of  $k$ -phase depends only on the distributions  $D_1, \dots, D_k$  and not the actual realizations



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## Problem Statement

### Problem Statement:

- Multi-armed bandit problem but each arm is pulled by a myopic agent
- An instance of the problem involves arms  $a_1, \dots, a_m$ , each having a persistent but a-priori random reward  $R_i$  drawn independently from distribution  $D_i$  with mean reward  $\mu_i$
- **Goal:** maximize expected reward

### Game Timeline:

- The rewards are drawn at the start of the game
- The agents begin arriving over time
- Agents receive some information from the mechanism and use it to decide which arm to pull
- They pull an arm, receive their reward, and exit the system
- The mechanism gets to observe the reward received by the agent and can use this observation to decide what to reveal to future agents



**Our Approach:** use information asymmetry to incentivize agents to explore, extending the results from [1]

[1] Kremer, Ilan, Yishay Mansour, and Motty Perry. "Implementing the "wisdom of the crowd"." *Journal of Political Economy* 122.5 (2014): 988-1012.

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## Our Mechanism (IPM)

1. Recommend  $a_1$  to the first agent
2. For each  $k \in \{2, \dots, m\}$ , begin the  $k$ -phase:
  - a) Partition  $D_{\max(k-1)}$  into intervals  $I_1, \dots, I_T$
  - b) Find the best arm  $i$  among  $\{1, \dots, k-1\}$
  - c) Find  $t \leq T$  such that  $r_i \in I_t$
  - d) For an agent  $j$ ,
    - i. If  $j < t$ , recommend  $a_i$
    - ii. If  $j = t$ , recommend  $a_k$
    - iii. If  $j > t$ , and  $r_k \geq r_i$ , recommend  $a_k$
    - iv. If  $j > t$ , and  $r_k < r_i$ , recommend  $\arg \max\{r_i, \mu_{k+1}\}$
3. Recommend the best arm after phases end

IPM is IC and always determines the best explorable\* arm

⇒ IPM attains constant regret w.r.t. the optimal offline mechanism whenever all arms are explorable

⇒ IPM attains constant regret w.r.t. the optimal IC mechanism unconditionally

We also show IPM achieves first-best whenever possible for an IC mechanism to do so

\* An arm  $a_i$  is *unexplorable* if another arm exceeds its mean reward with certainty. No IC mechanism can explore such arm

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